
Simulating the combustion of gaseous fuels

6th OpenFoam Workshop Training Session

Dominik Christ

This presentation shows how to use OpenFoam to simulate gas phase combustion



Overview

Theory

Tutorial case

Solution strategies

Validation

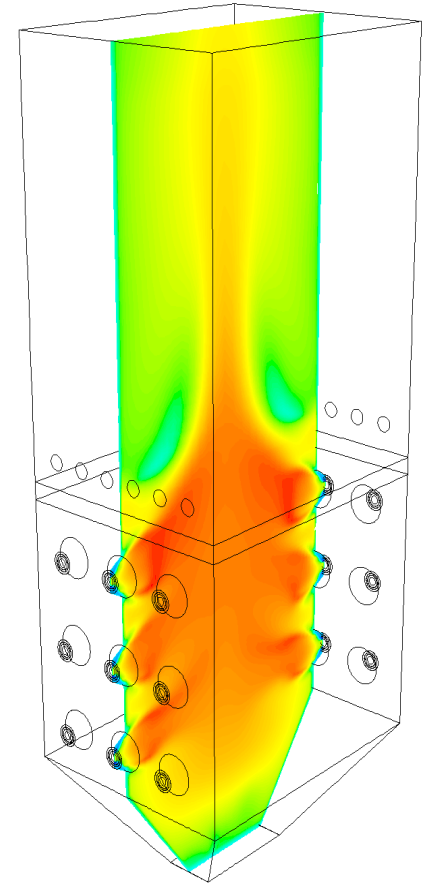
The focus of combustion simulation depends on the application



Burner design



Pollutant formation

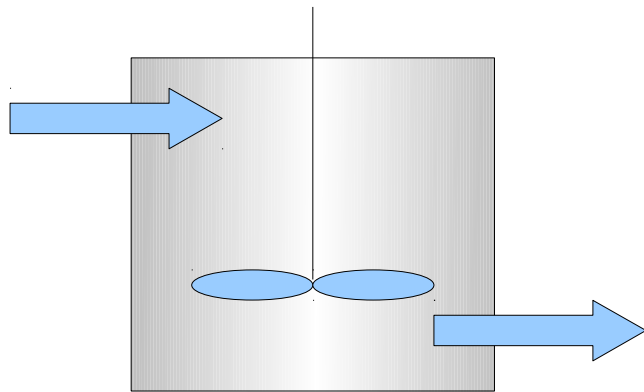


Furnace operation/retrofit

The focus of the present tutorial is simulating a model flame

- Model flames are a basis to test and evaluate combustion solvers
- Tutorial case is a turbulent methane/air flame (“Flame D” from Sandia/TNF workshop)
- Solver applications used are
 - rhoReactingFoam (PaSR model)
 - edcSimpleFoam (EDC model)
- Validation with experimental data to assess the solver/model accuracy





Overview

Theory (combustion; radiation)

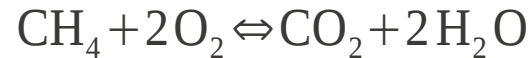
Tutorial case

Solution strategies

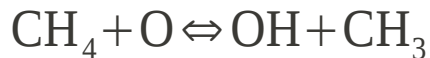
Validation

Combustion simulation is characterized by chemical reactions

Global reactions summarize the combustion process:



Detailed chemical mechanisms describe events on molecular level:



⋮

from GRI-Mech 3.0 (325 reactions, 53 species)

- *Chemical mechanisms need to be used within their specification limits, eg. GRI-Mech 3.0: methane/natural gas, T in 1000-2500 K, Φ in 0.1-5*
- *Detailed mechanism are more accurate (e.g. NO_x , ignition delay), but computationally much more expensive
→ level of detail needs to be chosen by the user*

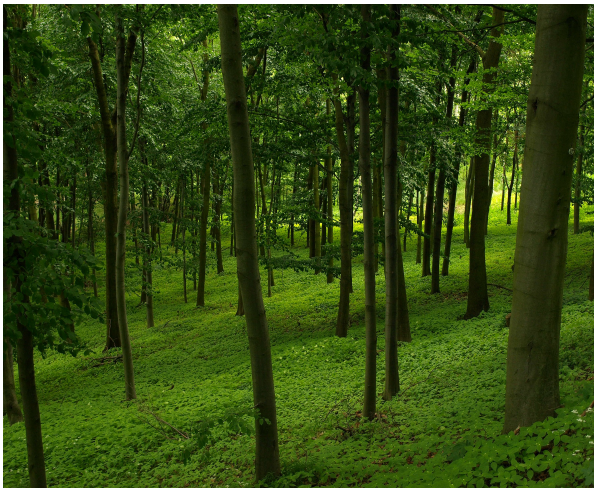
Chemical reactions can be described with equilibrium or kinetic rates (incl. “infinite rate”)

Equilibrium calculation depends only on thermodynamic data: h° , s° , cp°
But concerning combustion, many things are not in equilibrium!

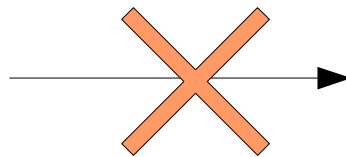
Chemical kinetics determine the reaction rate e.g. with an Arrhenius type formulation:

$$R = A T^b \exp\left(-\frac{E}{\mathcal{R} T}\right) C_{\text{CH}_4} C_{\text{O}_2}^{0.5}$$

“Infinite rate” chemistry is a special case, where reaction rates are assumed to be infinitely fast

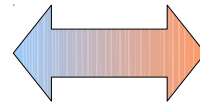


kinetically inhibited



In turbulent flows, turbulence/chemistry interaction defines the reacting flow

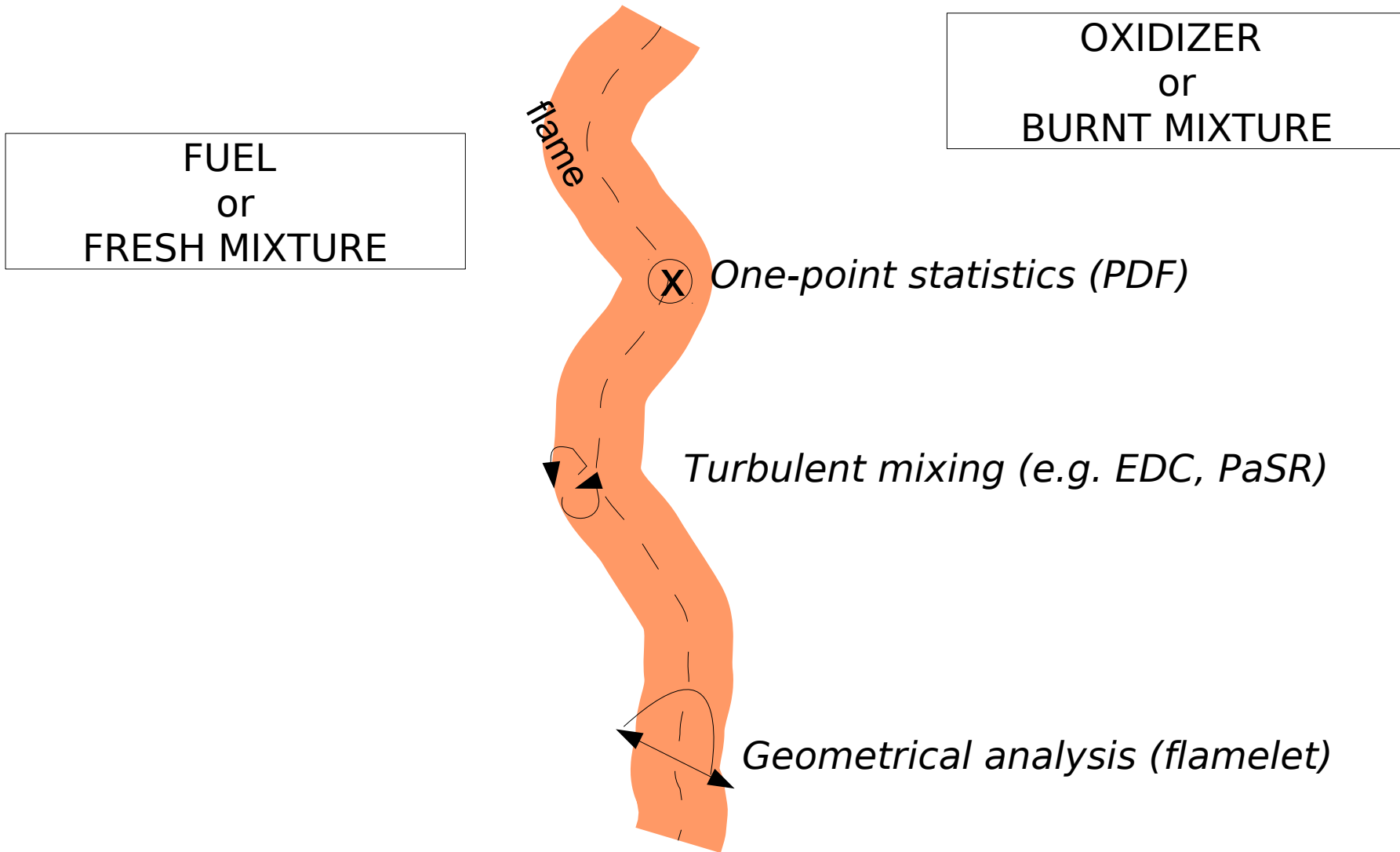
Turbulent flow



Chemical kinetics

- Turbulence enhances mixing of species such as fuel, oxidizer and products
- Strong turbulence can suppress combustion
→ local extinction
- In a laminar flow, combustion is controlled exclusively by chemical kinetics
- Combustion leads to flow acceleration
→ modification of flow field

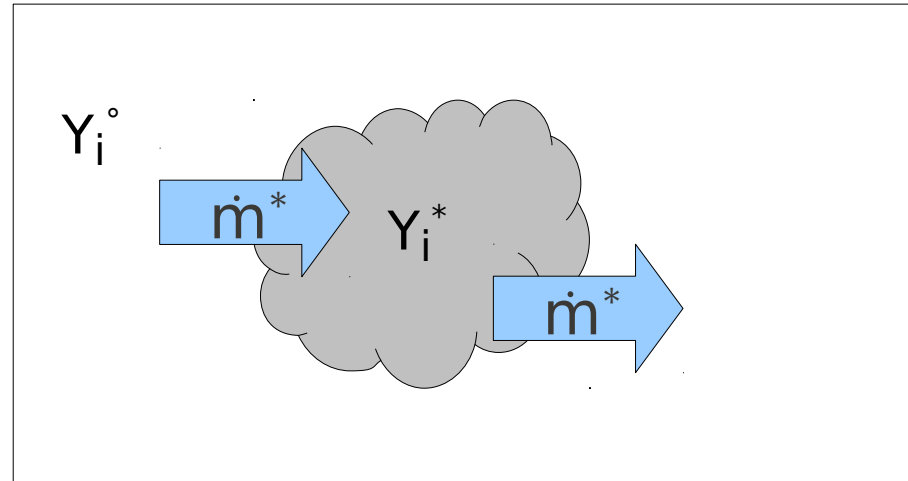
Different approaches exist to model the turbulence/chemistry interaction



cf. Poinso, Veynante "Theoretical and Numerical Combustion"

The Eddy-Dissipation Concept (EDC) assumes reactions in *fine structures*

$$\bar{R}_i = \bar{\rho} \frac{\gamma^* \dot{m}^*}{(1 - \gamma^*)} (\bar{Y}_i - Y_i^*)$$



Fraction of the flow occupied
by *fine structures*:

$$\gamma^*$$

Relation of mean, *fine structure*
and *surrounding* state:

$$\bar{Y}_i = \gamma^* Y_i^* + (1 - \gamma^*) Y_i^0$$

EDC reaction rate depends on turbulent flow properties and chemical kinetics approach

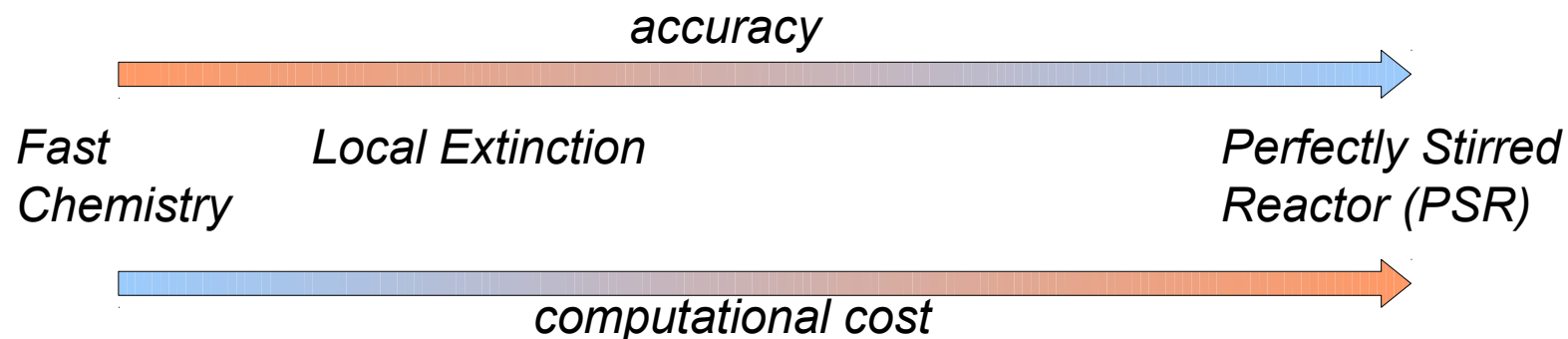
The fraction of the flow occupied by *fine structures*:

$$\gamma^* = 9.7 \left(\frac{\nu \cdot \epsilon}{k^2} \right)^{\frac{3}{4}}$$

Mass transfer rate between the *fine structures* and the *surroundings*:

$$\dot{m}^* = 2.45 \left(\frac{\epsilon}{\nu} \right)^{\frac{1}{2}}$$

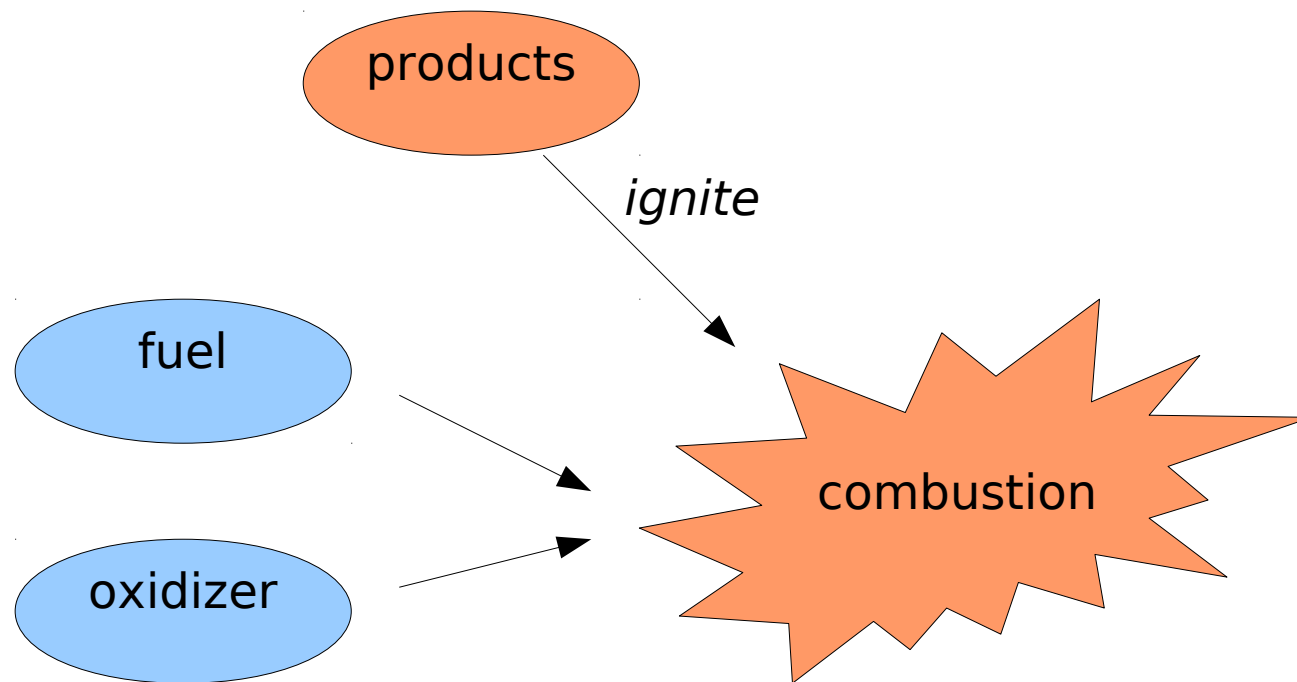
Chemical kinetics approaches for fine structure composition Y_i^* :



The Fast Chemistry approach assumes infinitely fast reactions

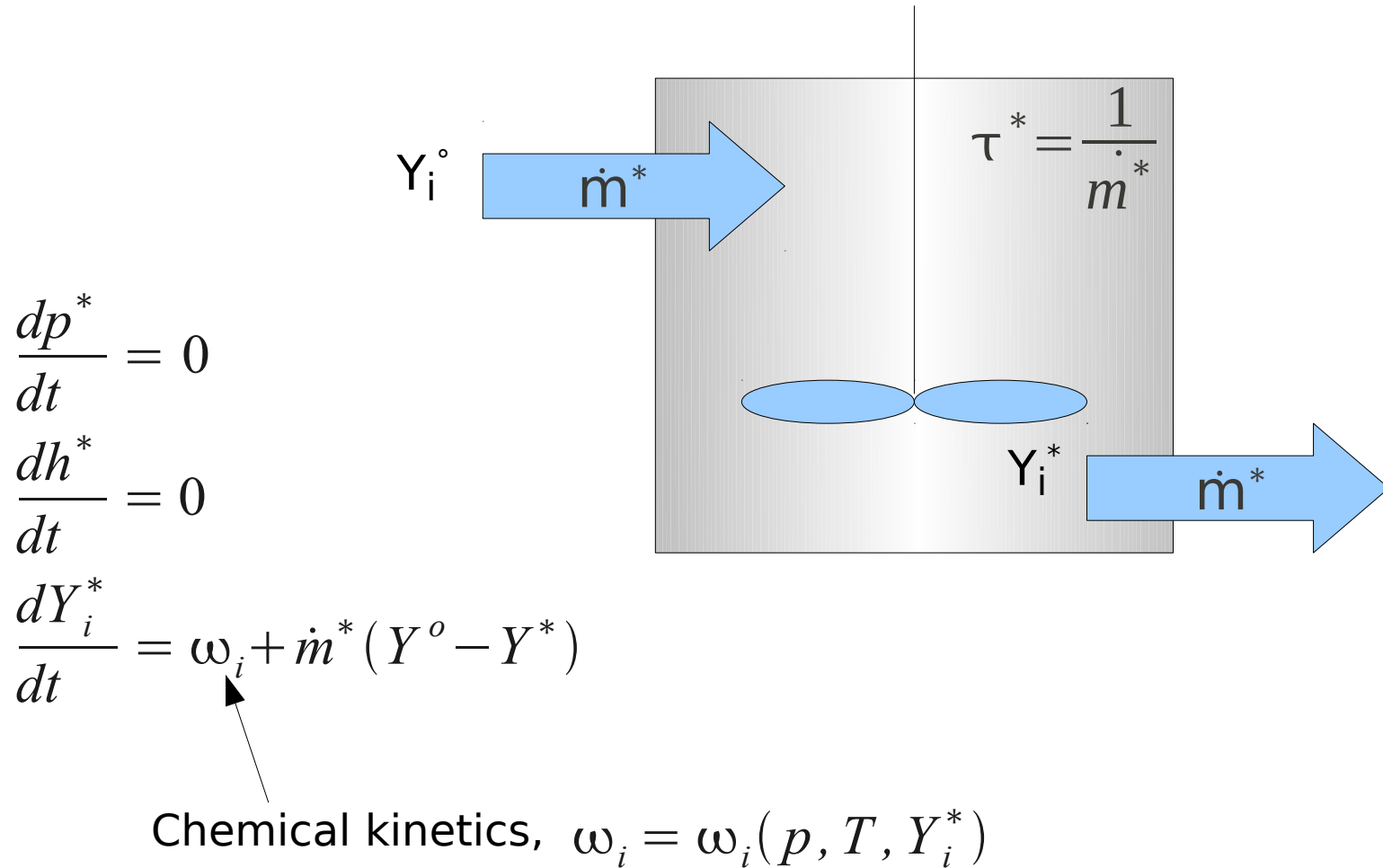
- Assumes sufficient time to achieve equilibrium inside fine structures
- Works only with irreversible global reactions

Combustion occurs if fuel, oxidizer and products meet simultaneously



→ *Product mass fractions must be initialized accordingly*

The PSR approach determines the steady-state of a perfectly stirred reactor



Local Extinction approach employs data from a priori PSR calculations

$$\tau^* < \tau_{ch} \Rightarrow R=0$$

τ_{ch} is the minimum residence time which sustains combustion in PSR.

Example 1:
Close to burner

high turbulence
($\tau^*=2.e-6$)

<

T = 300 K
($\tau_{ch}= 1.e-4$)

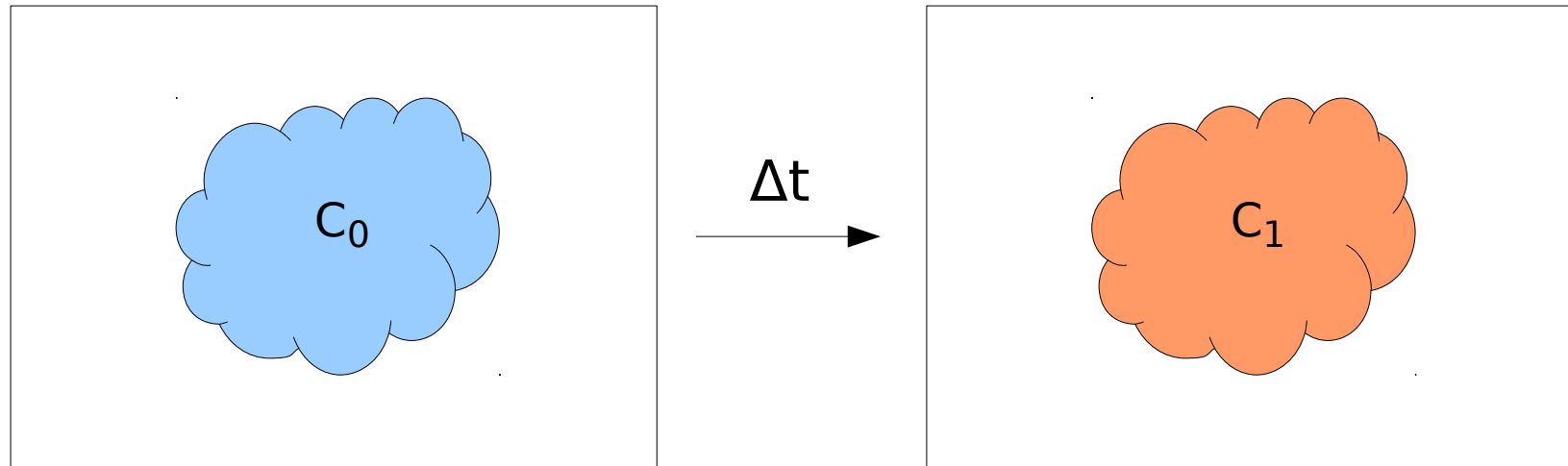
Example 2: Free
stream reaction zone

medium turbulence
($\tau^*=2.e-4$)

>

T = 900 K
($\tau_{ch}= 2.e-5$)

The PaSR combustion model derives the reaction rate in a transient manner



$$\bar{R}_i = \kappa \frac{C_{i,1} - C_{i,0}}{\Delta t}$$

Mixed fraction of cell that can react: κ

The parameter κ is based on two time scales

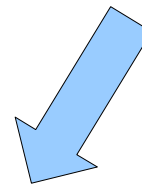
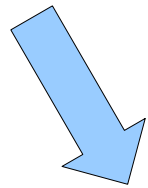
Turbulent mixing time scale:

$$\tau_m = \sqrt{\frac{k}{\epsilon} \left(\frac{\nu}{\epsilon} \right)^{\frac{1}{2}}}$$

Chemical time scale (infinite or finite rate):

$$\frac{1}{\tau_{ch}} = \max \left(-\frac{R_{fuel}}{\rho Y_{fuel}}, -\frac{R_{O_2}}{\rho Y_{O_2}} \right)$$

$$\frac{1}{\tau_{ch}} = -\frac{\partial R}{\rho \partial Y}$$



Mixed fraction that reacts:

$$\kappa = \frac{\tau_{ch}}{\tau_m + \tau_{ch}}$$

In OpenFOAM, mixing time scale is implemented slightly different

In rhoReactingFoam:

$$\tau_m = C_{mix} \sqrt{\frac{\mu_{eff}}{\rho \epsilon}}$$

In Chomiak (1996):

$$\tau_m = \sqrt{\frac{k}{\epsilon} \left(\frac{\nu}{\epsilon}\right)^{\frac{1}{2}}}$$

Both can be transformed into each other, using:

$$\frac{\mu_t}{\rho} = C_\mu \frac{k}{\epsilon}, \quad Sc_t = 1, \quad Re_t = \frac{k^2}{\epsilon \nu}$$

As result, we obtain:

$$C_{mix} = \sqrt{\frac{1}{1 + C_\mu Re_t}}$$

Chomiak (1996): *Flame Liftoff in Diesel Sprays* 25th Symp. Int. on Comb. pp. 2557-2564

The value for C_{mix} needs to be estimated a priori

$$C_{mix} = \sqrt{\frac{1}{1 + C_u Re_t}}$$

Laminar flow

$$Re_t = 0$$

$$C_{mix} = 1.0$$

Typical
turbulent flow

$$Re_t \approx 1000$$

$$C_{mix} \approx 0.1$$

Extremely
turbulent flow

$$Re_t \rightarrow \infty$$

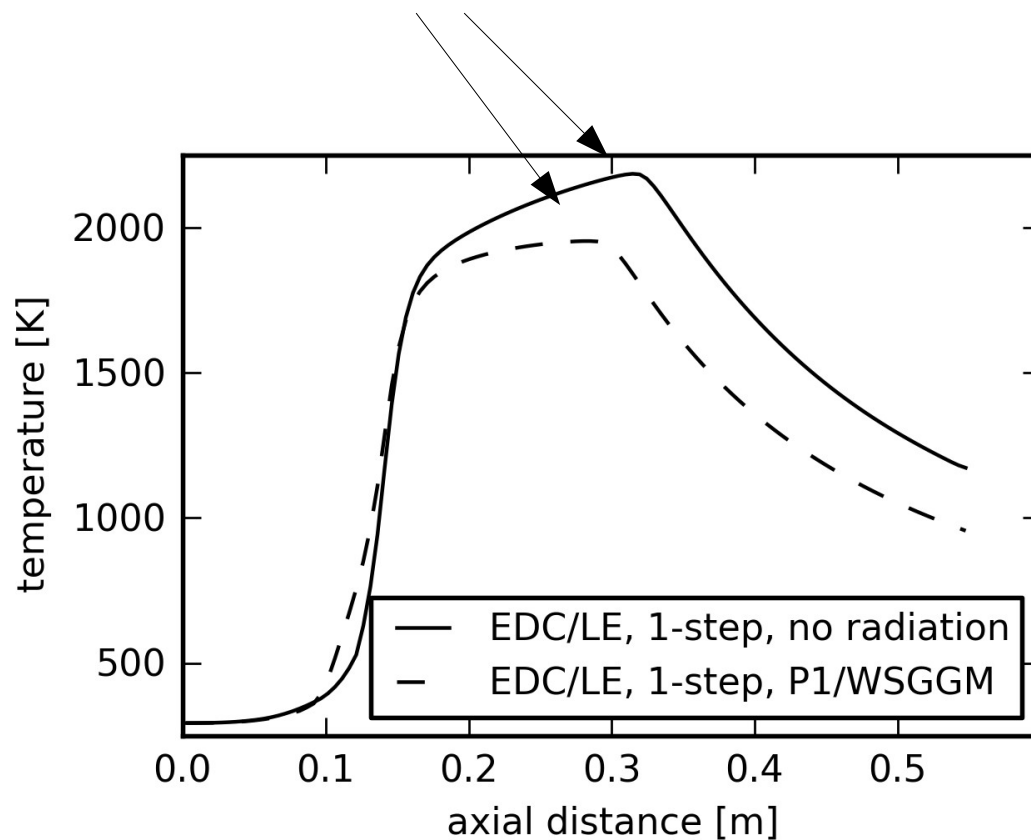
$$C_{mix} \rightarrow 0.0$$

Typical values for C_{mix} : 0.001 – 0.3; cf. Nordin (2001)

Nordin (2001): *Complex Chemistry Modelling of Diesel Spray Combustion*, PhD-Thesis

Radation heat transfer needs to be considered in combustion simulation

Peak temperature ≈ 250 K higher without radiation modelling



Radiation Transport Equation:

P1 - Transport

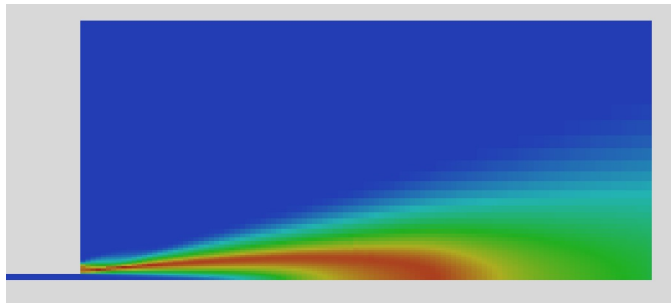
Discrete Ordinates (DOM)

Gas-Absorption Modelling:

constant

RADCAL-Polynomials

WSGGM (custom)



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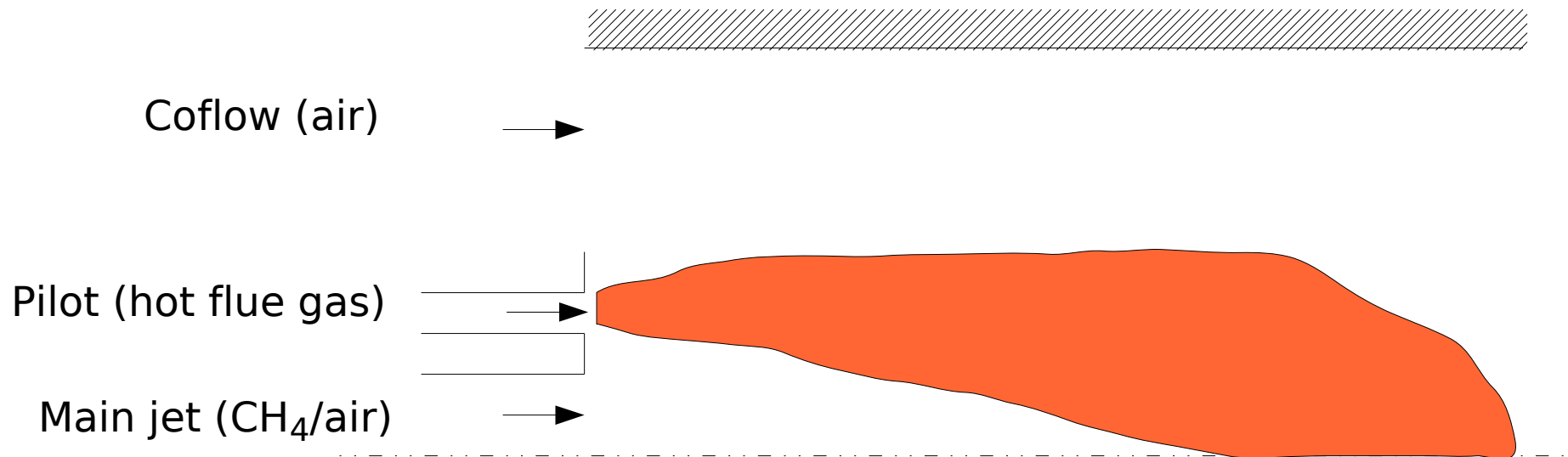
The tutorial case is a non-premixed piloted flame (“Flame D”)

Characteristics:

Steady-state, piloted, methane/air, diffusion flame, some local extinction

Geometry:

Axi-symmetric, 2D



The boundary conditions are identical for rhoReactingFoam and rhoSimpleFoam

	Ux [m/s]	p [Pa]	T [K]	Yi [-]	k [m ² /s ²]	epsilon [m ² /s ³]
Main jet	49.6	zeroGradient	294	fixedValue	$I_{\text{turb}}=0.0458$	$L_{\text{turb}}=5.04e-4$
Pilot	11.4	zeroGradient	1880	fixedValue	$I_{\text{turb}}=0.0628$	$L_{\text{turb}}=7.35e-4$
Coflow	0.9	zeroGradient	291	fixedValue	$I_{\text{turb}}=0.0471$	$L_{\text{turb}}=0.0197$
Outlet	zeroGradient	100000	zeroGradient	zeroGradient	zeroGradient	zeroGradient
Walls	0.0	zeroGradient	zeroGradient	zeroGradient	wall function	wall function

Front and backside of axi-symmetric domain are specified as 'wedge'.

edcSimpleFoam: Flow field initialized as required by chemical kinetics approach

- Fast Chemistry and Local Extinction: Set CO₂ and H₂O mass fraction to 0.01 everywhere.
- Perfectly Stirred Reactor: Initialize with Fast Chemistry or Local Extinction solution.
- Setup chemistryProperties:

```
edcFastChemCoeffs
{
    oxidiserName O2;
    mainFuelName CH4;
}
```

```
edcLECoeffs
{
    oxidiserName O2;
    mainFuelName CH4;
    autoIgnitionTemperature
        868;

    curve1
    {
        temperature 300;
        tauChMin 7.00E-005;
    }

    ...
}
```

```
edcPSRCoeffs
{
    relativeTolerance 1.e-6;
    absoluteTolerance 1.e-14;
    maxIterations 1.e8;

    useBinaryTree off;
    binaryTreeTolerance 1e-4;
    binaryTreeSize 1.e7;
}
```

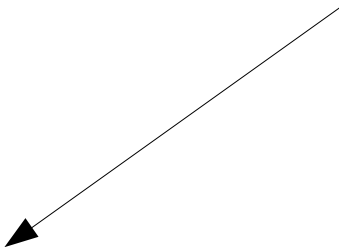
*no local extinction
above this
temperature*

rhoReactingFoam: Choosing C_{mix} and ODE intergrator

- Estimate turbulent Reynolds number:

$$Re_t=500 \rightarrow C_{mix} = 0.15$$

*SIBS is stable
enough for solving
detailed chemistry*



- Setup chemistryProperties:

```
odeCoeffs
{
    ODESolver      SIBS;
    eps            5.0e-4;
    scale          1.0;
}
```


Setting-up discretization schemes

- *Convective term*: Linear upwind discretization (2nd order accurate)
default Gauss linearUpwind cellLimited Gauss linear 1;

For species Y_i (for rhoReactionFoam: Y_i and hs)

```
div(phi,Yi) Gauss multivariateSelection
{
    //hs    linearUpwind cellLimited Gauss linear 1;
    CH4    linearUpwind cellLimited Gauss linear 1;
    O2     linearUpwind cellLimited Gauss linear 1;
    ...
}
```

- *Time discretization*: (Pseudo) steady-state
edcSimpleFoam (steady-state solver)
default steadyState;
rhoReactingFoam (transient solver)
default SLTS phi rho 0.7;
default CoEuler phi rho 0.4;
- global under-relaxation factor* →
- *max. CFL number*

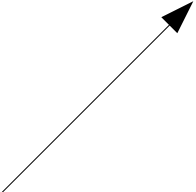
Setting-up fvSolution

Numerical solver precision depends on solver type:

Transient solver requires each time-step to be accurate
all variables: $\text{relTol} = 0.;$

Steady state solver can reach solution through intermediate results
pressure: $\text{relTol } 0.001;$
other variables: $\text{relTol } 0.1;$

intermediate results will not be accurate

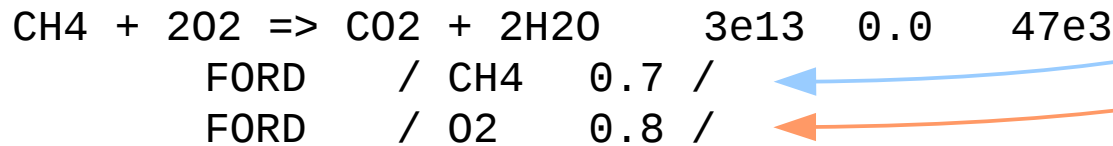


Chemical mechanisms can be defined in Chemkin or OpenFOAM native format

Example: Arrhenius type kinetics

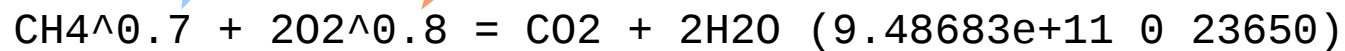
$$R = A T^b \exp\left(-\frac{E}{RT}\right) C_{\text{CH}_4}^{0.7} C_{\text{O}_2}^{0.8}$$

Chemkin format uses units: mol, cm³, s, K; cal

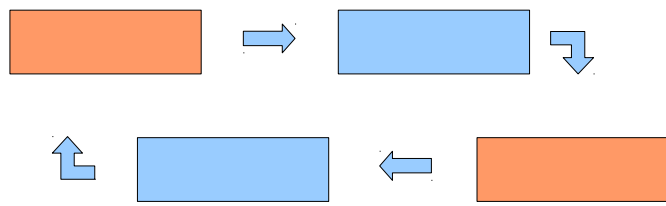


OpenFoam native format uses units: kmol, m³, s, K; K

irreversibleArrheniusReaction



Use chemkinToFoam to convert chemkin files (or to check their consistency)



Overview

Theory

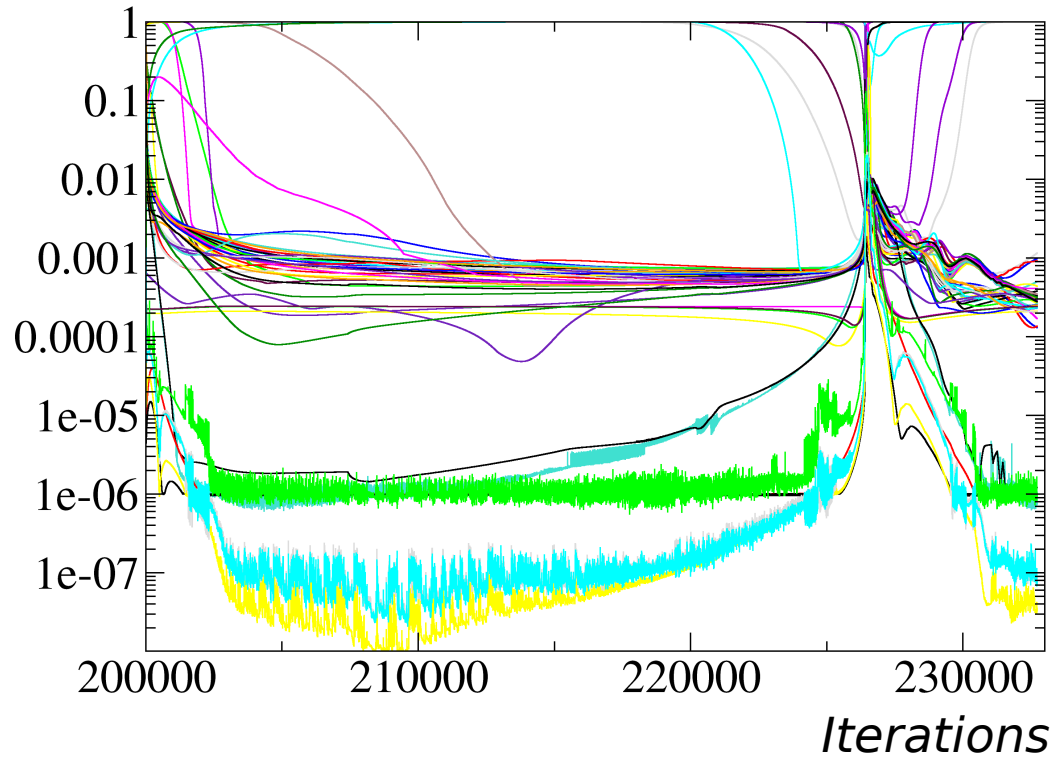
Tutorial case

Solution strategies

Validation

Combustion simulation often faces stability issues

Residuals



Many error sources are possible because numerous models are applied simultaneously, for example:

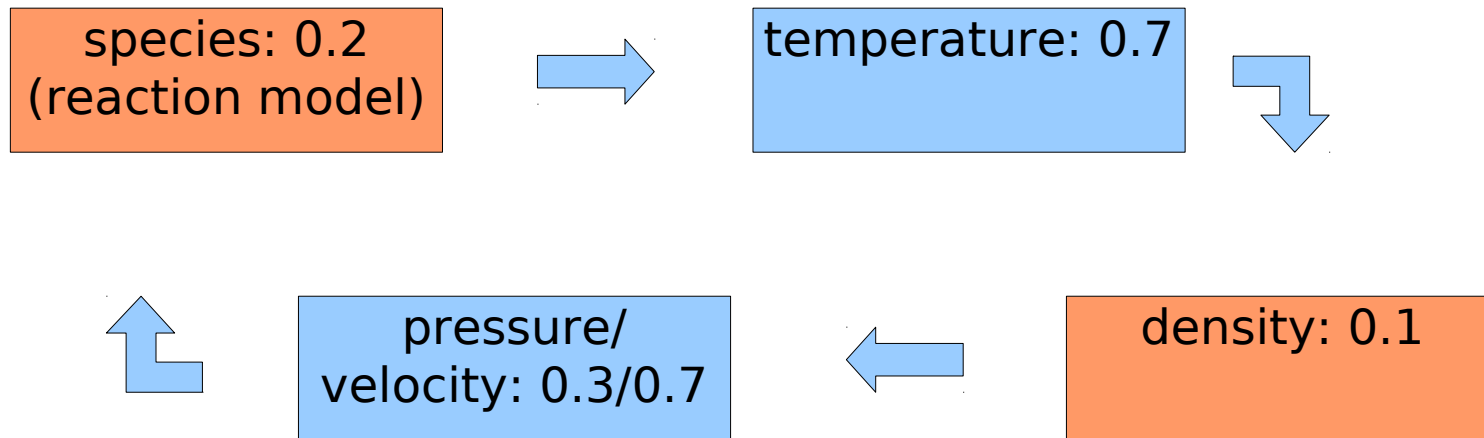
- Compressible flow
- Coupling of transport equations
- Numerically stiff reaction mechanisms

Solution strategies include good initialization and under-relaxation

Possible “well initialized” flow fields are:

- Cold flow
- Starting solution (steady-state; 1- or 2-Step)
- Products

Strong coupling between transport equations may be broken with different under-relaxation factors.



*Under-relaxation only applicable to steady-state cases.
Unsteady solver based on Transient-SIMPLER needed?*

Tabulation of PSR reactor results can provide speed-up and additional stability

$$\begin{pmatrix} \gamma^* \\ m^* \\ Y_1 \\ \vdots \\ Y_n \end{pmatrix}$$

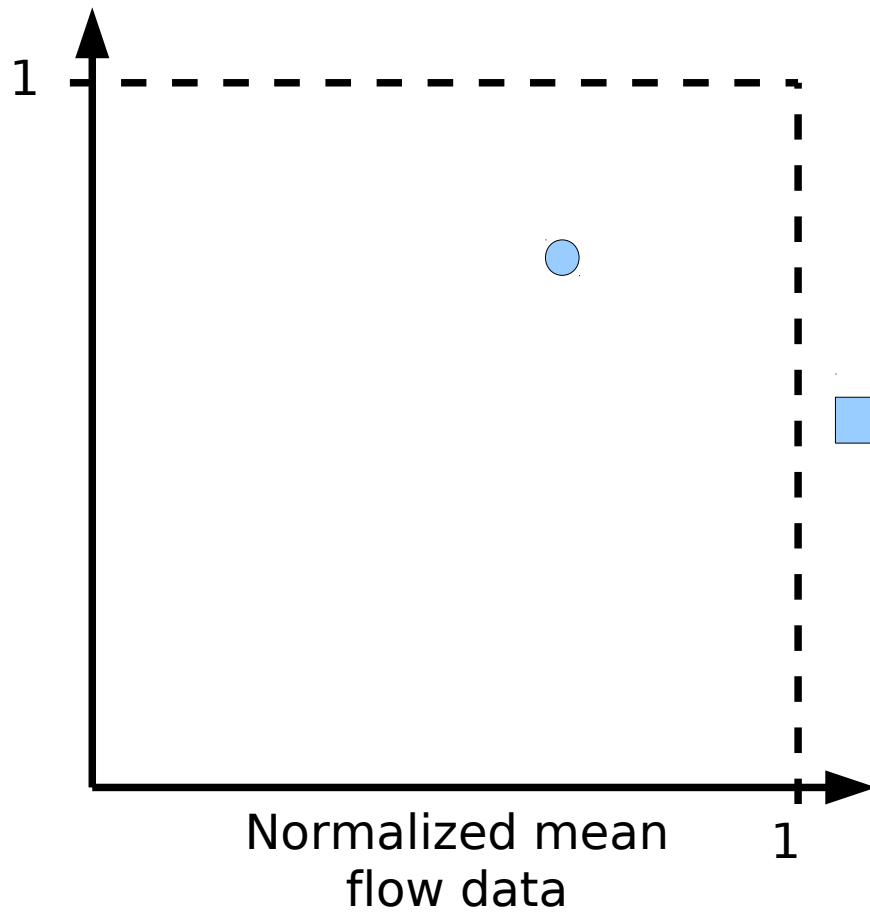
Mean flow data



$$\begin{pmatrix} T^* \\ Y_1^* \\ \vdots \\ Y_n^* \end{pmatrix}$$

PSR integration results

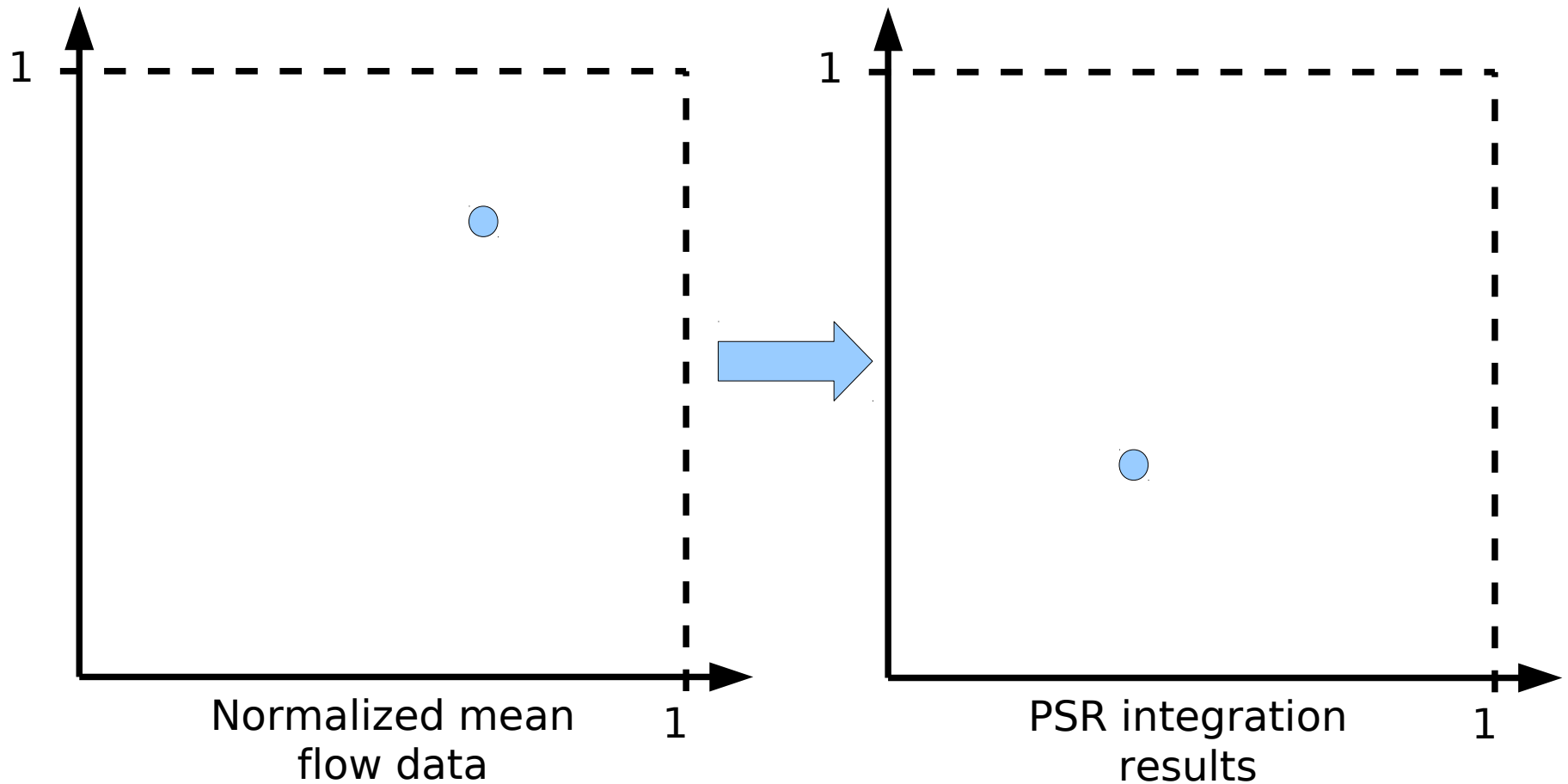
Tabulation of PSR reactor results can provide speed-up and additional stability



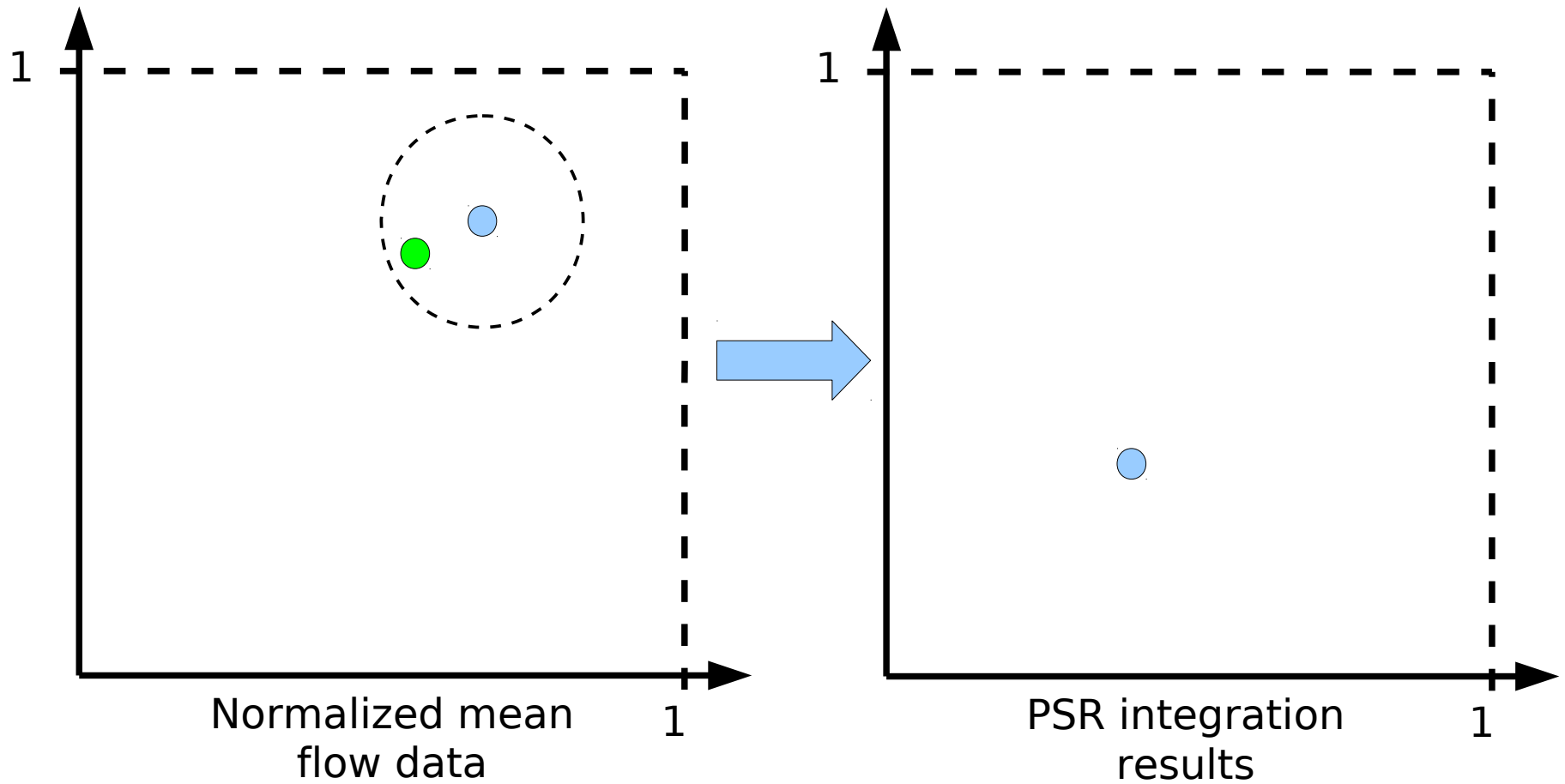
$$\begin{pmatrix} T^* \\ Y_1^* \\ \vdots \\ Y_n^* \end{pmatrix}$$

PSR integration results

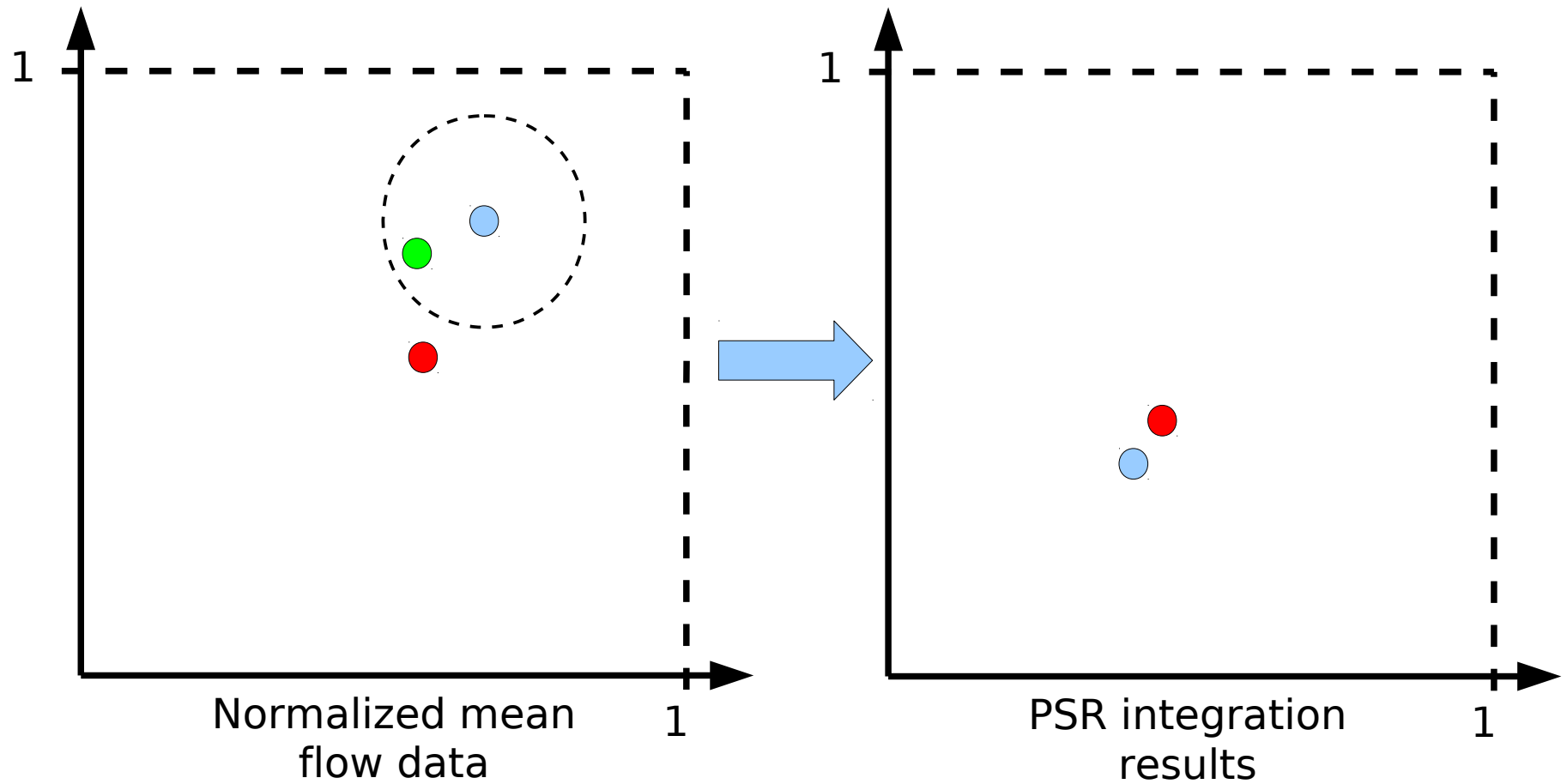
Tabulation of PSR reactor results can provide speed-up and additional stability



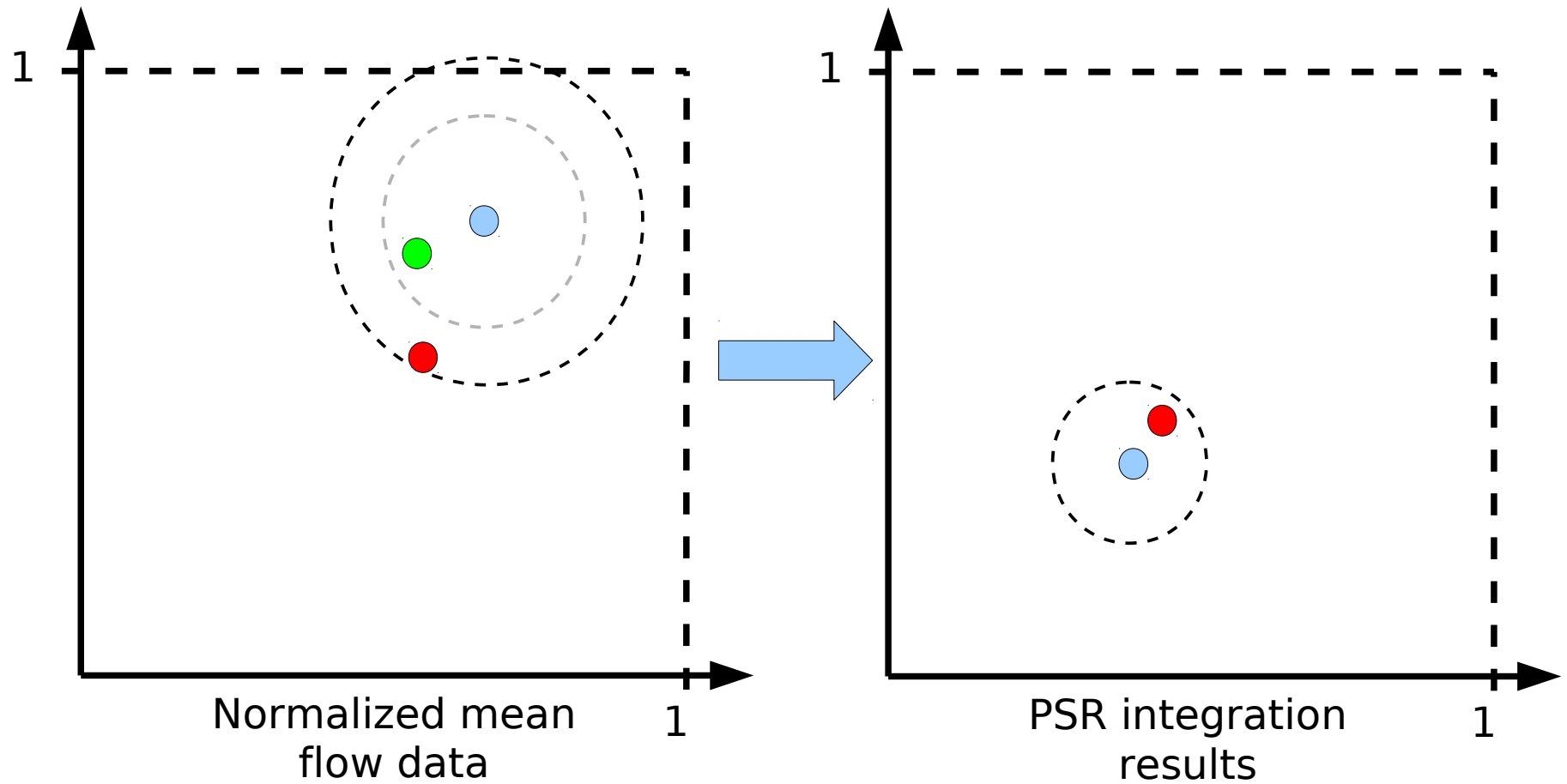
Tabulation of PSR reactor results can provide speed-up and additional stability



Tabulation of PSR reactor results can provide speed-up and additional stability



Tabulation of PSR reactor results can provide speed-up and additional stability



Limiting temperature is possible in steady-state cases

In a steady state case, intermediate “time steps” are not accurate.
→ Temperature may temporarily increase and needs to be limited

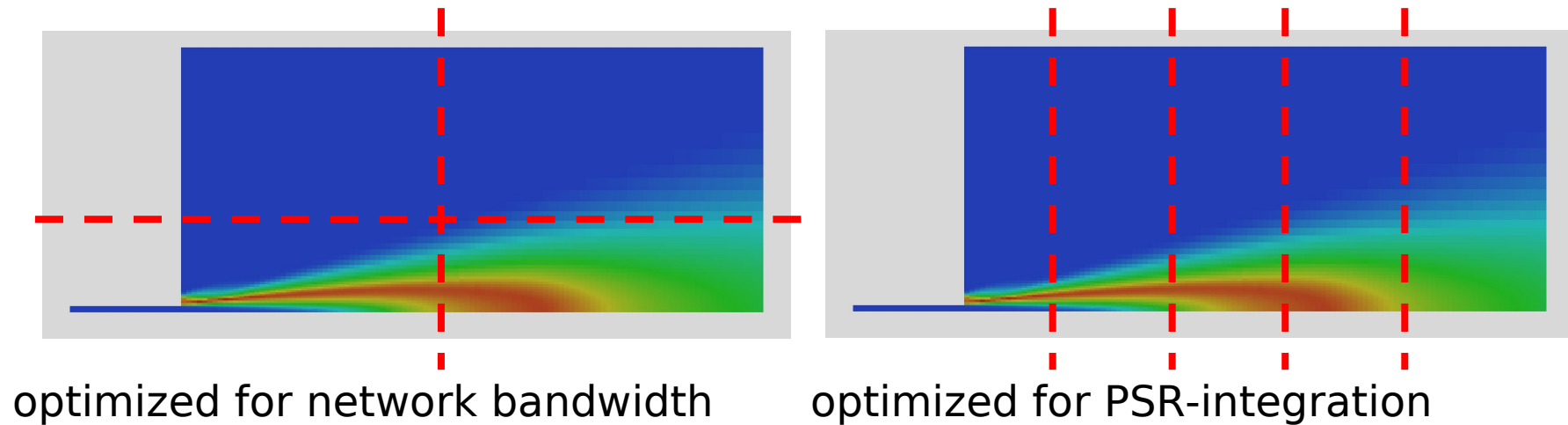
Solver level implementation in edcSimpleFoam:

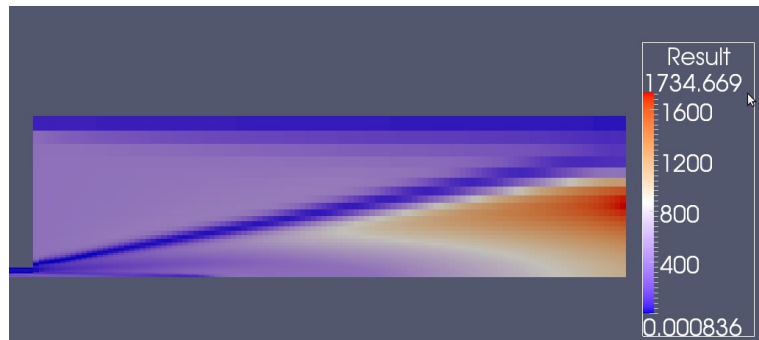
- New enthalpy field calculated from species mass fractions and T_{\min}
- Another enthalpy field calculated for T_{\max}
- Both fields are used to limit enthalpy field
- T_{\max} and T_{\min} are specified in `thermophysicalProperties`

Request for integrated limitation filed in OpenCFD's bugtracker (Issue #57).

Optimal parallelization depends on the complexity of the chemical model

Integrating complex chemical mechanisms is computationally much more expensive than solving transport equations (even if there are many)!





Overview

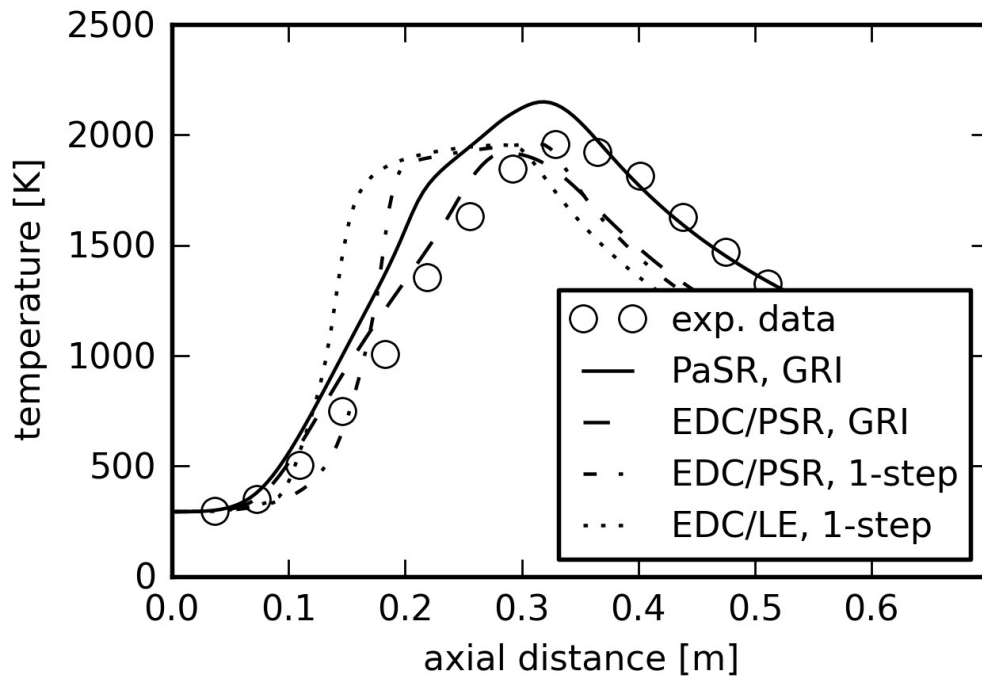
Theory

Tutorial case

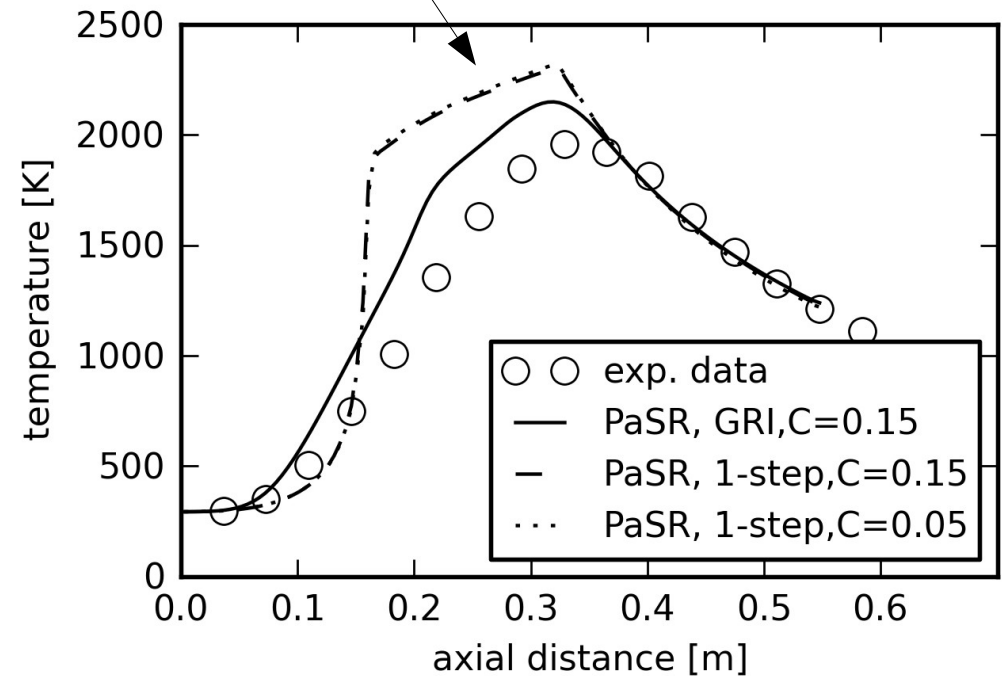
Solution strategies

Validation

Detailed reaction mechanism predicts temperature profile accurately



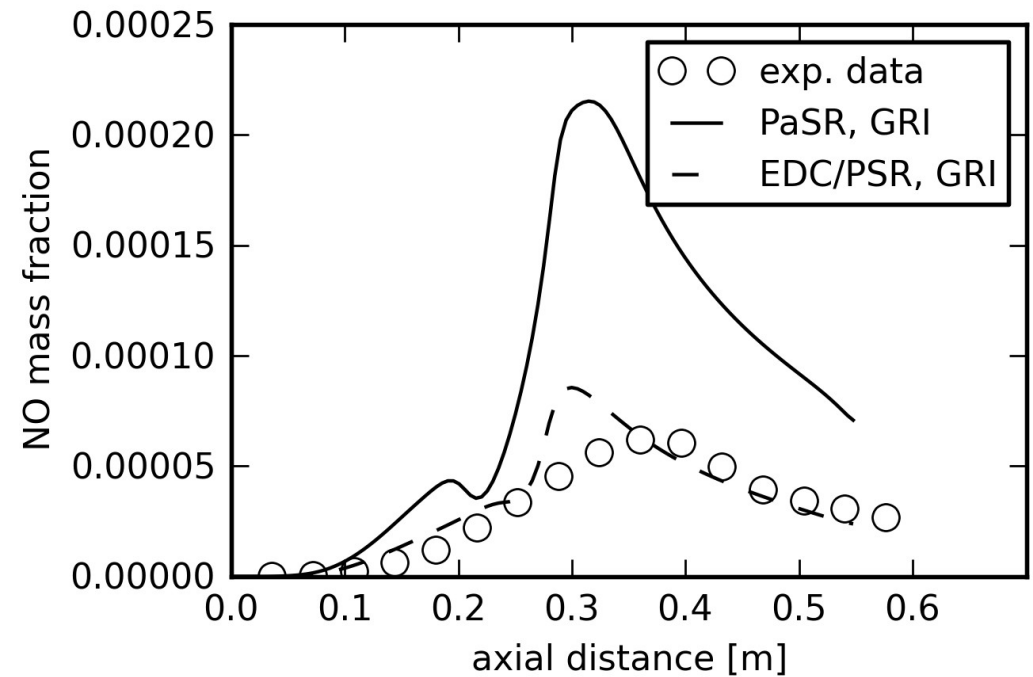
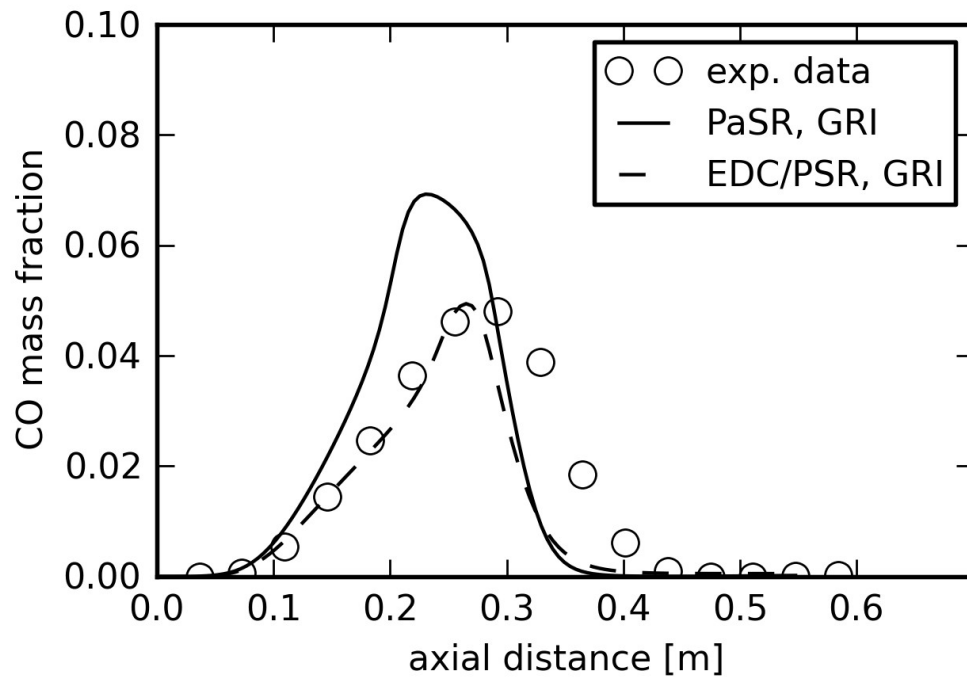
Influence of C_{mix} is minimal



Radiation modeling used with EDC, not used with PaSR.

exp. data: Barlow, R. S. and Frank, J. H., Proc. Combust. Inst. 27:1087-1095 (1998)

Intermediate species and pollutants are more difficult to predict



ParaFoam's "calculator" can be used to check Re_t assumption

The image shows the ParaFoam calculator interface. A callout box highlights the calculator's input field, which contains the mathematical expression $k^2/\epsilon \cdot \rho/\mu$. Below the input field are buttons for "Clear", "(", ")", and "iHat". The main interface shows the same expression entered into the calculator, with a "Result" field displaying the value 1734.669. To the right of the calculator is a heatmap visualization of the flow field, with a color scale ranging from 0.000836 (blue) to 1734.669 (red). The heatmap shows a turbulent flow field with a high-velocity region (red) and a low-velocity region (blue).

Attribute Mode: Cell Data

Coordinate Results

Result Array Name: Result

$k^2/\epsilon \cdot \rho/\mu$

Clear () iHat

Apply Reset Delete ?

Attribute Mode: Cell Data

Coordinate Results

Result Array Name: Result

$k^2/\epsilon \cdot \rho/\mu$

Clear	()	iHat	jHat	kHat	/
sin	cos	tan	7	8	9	*
asin	acos	atan	4	5	6	-
sinh	cosh	tanh	1	2	3	+
x^y	sqrt	exp	ln	log10	0	.
ceil	floor	abs	Scalars			▼
v1.v2	mag	norm	Vectors			▼

Replace invalid results

Replacement value: 0

Result: 1734.669

Color scale: 0.000836 to 1734.669

Comparison with measurements may require special post-processing

Common difficulties when comparing simulated mass fractions with measurements:

- Measured data are often mole fractions or concentrations
If not all (major) species are measured, correct conversion to mass fractions impossible
- Flue gas or emission monitoring can be measured in “dry gas”, i.e. after water vapor has been condensed out
Simulated data comprise a complete set, therefore they can be accurately converted

New utility massToMoleFraction handles conversion together with “-dryGas” option

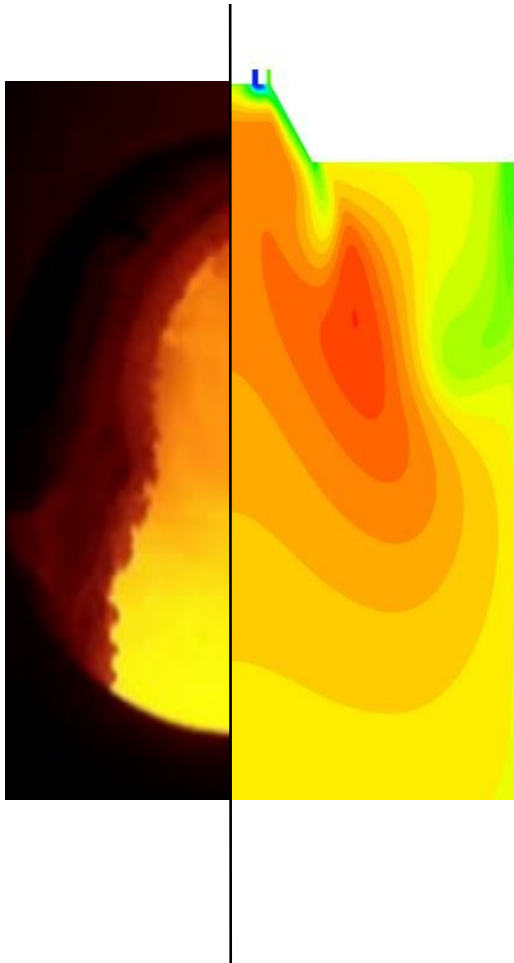
Final note: When using edcSimpleFoam or edcPisoFoam, please cite

for the EDC model:

B. Magnussen: *The Eddy Dissipation Concept: A Bridge between Science and Technology*, ECCOMAS Thematic Conference on Computational Combustion, Lisbon, Portugal, 2005

for the validation of the OpenFoam implementation:

B. Lilleberg, D. Christ, I.S. Ertesvåg, K.E. Rian, R. Kneer, *Numerical simulation with an extinction database for use with the Eddy Dissipation Concept for turbulent combustion* (submitted)



Thank you for your attention!